

Unit 6 Practice Exam 2017

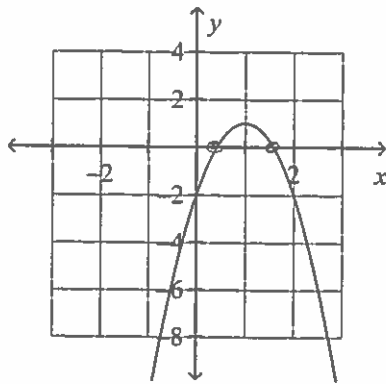
Multiple Choice

Identify the choice that best completes the statement or answers the question.

- A 1. Which of the quadratic functions has the widest graph?
- a. $y = -\frac{1}{2}x^2$ b. $y = -5x^2$ c. $y = -3x^2$ d. $y = -\frac{7}{8}x^2$

- A 2. A parabola _____ has an axis of symmetry.
- a. always b. sometimes c. never

- B 3. For which discriminant is the graph possible?



2 roots \Rightarrow Pos #

- a. $b^2 - 4ac = 0$ b. $b^2 - 4ac = 10$ c. $b^2 - 4ac = -8$

Name: _____

$$\begin{aligned} a &= -1 \\ b &= -1 \\ c &= -1 \end{aligned}$$

AOS: $x = \frac{-(-1)}{2(-1)} = \frac{1}{-2} = -\frac{1}{2}$ or -0.5

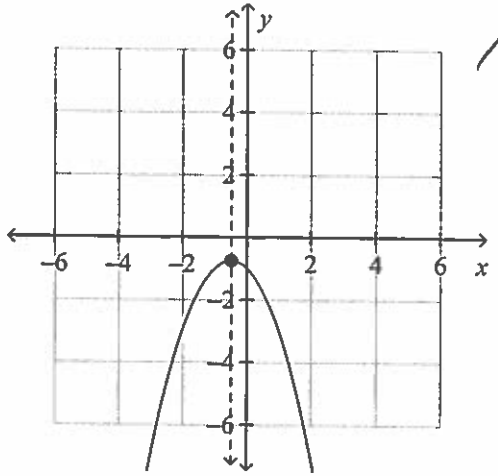
$y = -(-0.5)^2 - (-0.5)$

$y = -(-0.5)^2 - (-0.5)$
 $y = -0.75$

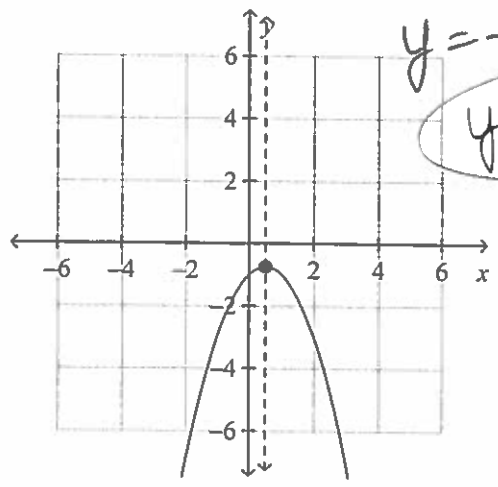
B

4. Graph $f(x) = -x^2 - x - 1$. Label the axis of symmetry and vertex.

a.

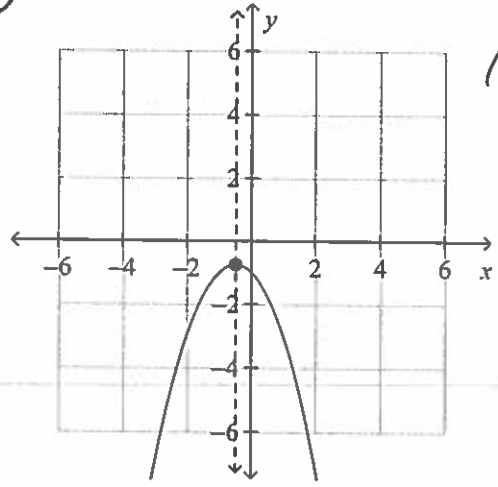


Axis of symmetry: $x = -0.5$
 Vertex: $(-0.5, -0.75)$



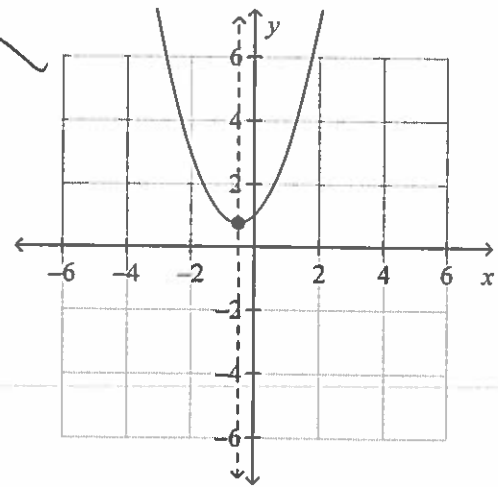
Axis of symmetry: $x = 0.5$
 Vertex: $(0.5, -0.75)$

b.



Axis of symmetry: $x = -0.5$
 Vertex: $(-0.5, -0.75)$

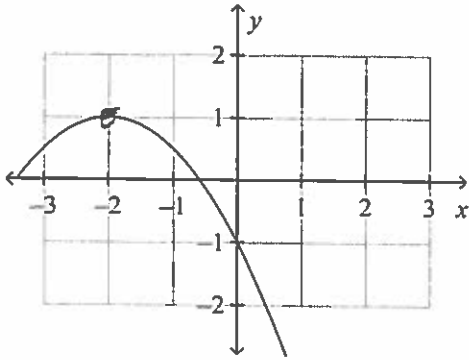
d.



Axis of symmetry: $x = -0.5$
 Vertex: $(-0.5, 0.75)$

Short Answer

5. Identify the vertex of the graph. Tell whether it is a minimum or maximum.



V (-2, 1)
Maximum

6. Order the group of quadratic functions from widest to narrowest graph.

$y = -2x^2, y = \frac{2}{3}x^2, y = -\frac{1}{4}x^2$

Widest Middle Narrowest
 $y = -\frac{1}{4}x^2, y = \frac{2}{3}x^2, y = -2x^2$

Solve the equation using square roots.

7. $x^2 + 30 = 5$
 $-30 - 30$
 $x^2 = -25$

0 roots —
no solution

Use any method to solve the equation. If necessary, round to the nearest hundredth.

8. $6x^2 - 31 = 0$

$\frac{6x^2}{6} = \frac{31}{6}$
 $x^2 = \sqrt{5.16}$

$x = \pm 2.27$

Using the discriminant, find the number of real number solutions for the equation.

9. $x^2 + 3x + 3 = 0$

$b^2 - 4ac$
 $(3)^2 - 4(1)(3)$
 $9 - 12 = -3$

0 roots

10. Find the equation of the axis of symmetry and the coordinates of the vertex of the graph of the function.

$y = 2x^2 + 4x - 3$

AXIS OF SYMMETRY: $x = -1$ VERTEX: $(-1, -5)$

$x = \frac{-4}{2(2)} = \frac{-4}{4} = -1$ $y = 2(-1)^2 + 4(-1) - 3$
 $= 2 - 4 - 3$
 $y = -5$

11. Solve the equation using square roots. $x^2 - 4 = -10$

$$\begin{array}{r} x^2 - 4 = -10 \\ +4 \quad +4 \\ \hline x^2 = -4 \end{array}$$

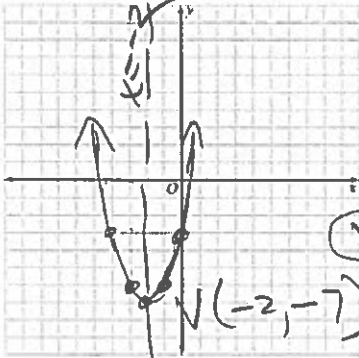
$x = \pm 2$

12. Solve the equation using square roots. $3x^2 = 54$

$$\begin{array}{r} 3x^2 = 54 \\ \frac{3}{3} \quad \frac{3}{3} \\ \hline x^2 = 18 \end{array}$$

$x = \pm 4.24$

13. Graph $f(x) = x^2 + 4x - 3$



AOS: $x = \frac{-4}{2(1)} = \frac{-4}{2} = -2$

$x = -2$

x	$(x)^2 + 4(x) - 3$	y
-4	$(-4)^2 + 4(-4) - 3$	-3
-3	$(-3)^2 + 4(-3) - 3$	-6
\checkmark -2	$(-2)^2 + 4(-2) - 3$	-7
-1	$(-1)^2 + 4(-1) - 3$	-6
0	$(0)^2 + 4(0) - 3$	-3

14. Solve the equation by quadratic formula or factoring. $z^2 + 2z - 8 = 0$

$z = 1$
 $z = 2$
 $z = -8$

$$z = \frac{-2 \pm \sqrt{(2)^2 - 4(1)(-8)}}{2} = \frac{-2 \pm \sqrt{4 + 32}}{2}$$

$$= \frac{-2 \pm \sqrt{36}}{2} = \frac{-2 \pm 6}{2}$$

$\frac{-2+6}{2} = \frac{4}{2} = 2$
 $\frac{-2-6}{2} = \frac{-8}{2} = -4$

$$(z+4)(z-2) = 0$$

$z+4=0 \Rightarrow z=-4$
 $z-2=0 \Rightarrow z=2$

15. Solve the equation by quadratic formula or factoring. $2x^2 + 7x - 15 = 0$

$2x^2 - 3x$	$-10x - 15$
$+10x - 15$	

$$-30x^2 (2x-3)(x+5) = 0$$

$2x-3=0 \Rightarrow x=1.5$
 $x+5=0 \Rightarrow x=-5$

$$x = \frac{-7 \pm \sqrt{(7)^2 - 4(2)(-15)}}{2(2)}$$

$$= \frac{-7 \pm \sqrt{49 + 120}}{4} = \frac{-7 \pm \sqrt{169}}{4} = \frac{-7 \pm 13}{4}$$

$\frac{-7+13}{4} = \frac{6}{4} = \frac{3}{2}$
 $\frac{-7-13}{4} = \frac{-20}{4} = -5$

16. Use the discriminant to find the number of solutions for the equation. $x^2 + 15 = 0$

(YOU DO NOT HAVE TO SOLVE.)

$a=1$
 $b=0$
 $c=15$

$$b^2 - 4ac = (0)^2 - 4(1)(15) = 0 - 60 = -60$$

-60 0 roots

17. Use the discriminant to find the number of solutions for the equation. $x^2 - 16x + 60 = 0$

(YOU DO NOT HAVE TO SOLVE.)

$a=1$
 $b=-16$
 $c=60$

$$(-16)^2 - 4(1)(60) = 256 - 240 = 16$$

16 2 roots

18. Use the Quadratic Formula to solve the equation. $9x^2 + 4x - 16 = 0$

$a=9$
 $b=4$
 $c=-16$

$$x = \frac{-4 \pm \sqrt{(4)^2 - 4(9)(-16)}}{2(9)} = \frac{-4 \pm \sqrt{16 + 576}}{18} = \frac{-4 \pm \sqrt{592}}{18}$$

$$= \frac{-4 \pm 24.33}{18} \left\{ \begin{array}{l} \frac{20.33}{18} = 1.13 \\ \frac{-28.33}{18} = -1.57 \end{array} \right.$$

19. Use quadratic formula or factoring to solve the equation. $x^2 - 3x - 4 = 0$

$a=1$
 $b=-3$
 $c=-4$

$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(1)(-4)}}{2(1)} = \frac{3 \pm \sqrt{9 + 16}}{2} = \frac{3 \pm 5}{2}$$

$$= \frac{3+5}{2} = \frac{8}{2} = 4$$

$$= \frac{3-5}{2} = \frac{-2}{2} = -1$$

$(x-4)(x+1) = 0$
 $x-4=0 \Rightarrow x=4$
 $x+1=0 \Rightarrow x=-1$

20. Use quadratic formula or factoring to solve the equation. $3x^2 - 6x - 24 = 0$

$3x^2 - 6x - 24 = 0$
 $x^2 - 2x - 8 = 0$
 $(x-4)(x+2) = 0$
 $x-4=0 \Rightarrow x=4$
 $x+2=0 \Rightarrow x=-2$

$a=3$
 $b=-6$
 $c=-24$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(3)(-24)}}{2(3)} = \frac{6 \pm \sqrt{36 + 288}}{6} = \frac{6 \pm \sqrt{324}}{6} = \frac{6 \pm 18}{6}$$

$$= \frac{6+18}{6} = 4$$

$$= \frac{6-18}{6} = -2$$

21. Use quadratic formula or factoring to solve the equation. $-3y^2 - 5y + 8 = 0$

$a=-3$
 $b=-5$
 $c=8$

$$y = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(-3)(8)}}{2(-3)} = \frac{5 \pm \sqrt{25 + 96}}{-6} = \frac{5 \pm \sqrt{121}}{-6} = \frac{5 \pm 11}{-6}$$

$$= \frac{5+11}{-6} = \frac{16}{-6} = -2\frac{2}{3}$$

$$= \frac{5-11}{-6} = \frac{-6}{-6} = 1$$

Solve the equation by quadratic formula or factoring.

22. $-12 = -3x^2 + 9x$

$$-3x^2 + 9x + 12 = 0$$

$a=-3$
 $b=9$
 $c=12$

$$x = \frac{-9 \pm \sqrt{(9)^2 - 4(-3)(12)}}{2(-3)} = \frac{-9 \pm \sqrt{81 + 144}}{-6} = \frac{-9 \pm \sqrt{225}}{-6} = \frac{-9 \pm 15}{-6}$$

$$= \frac{-9+15}{-6} = \frac{6}{-6} = -1$$

$$= \frac{-9-15}{-6} = \frac{-24}{-6} = 4$$

$x^2 - 3x - 4 = 0$
 $(x-4)(x+1) = 0$
 $x-4=0 \Rightarrow x=4$
 $x+1=0 \Rightarrow x=-1$

Solve the equation by quadratic formula. Round to the nearest hundredth if necessary.

23. $x^2 + 6x - 10 = 0$

$a=1$
 $b=6$
 $c=-10$

$$x = \frac{-6 \pm \sqrt{(6)^2 - 4(1)(-10)}}{2(1)} = \frac{-6 \pm \sqrt{36 + 40}}{2} = \frac{-6 \pm \sqrt{76}}{2}$$

$$= \frac{-6 \pm 8.72}{2}$$

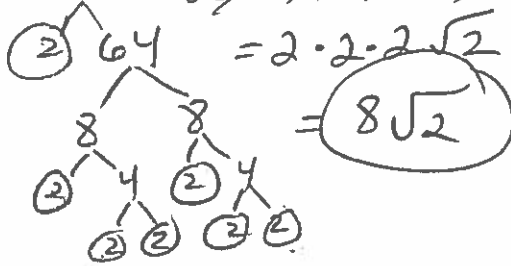
$$= \frac{-6+8.72}{2} = \frac{2.72}{2} = 1.36$$

$$= \frac{-6-8.72}{2} = \frac{-14.72}{2} = -7.36$$

Name: _____

A

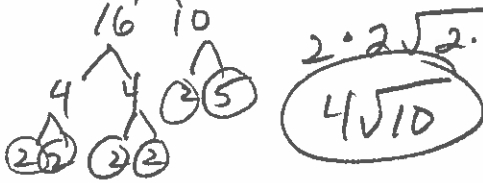
24. Simplify the radical expression. $\sqrt{128} = \sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2}$



OR $\sqrt{64 \cdot 2} = 8\sqrt{2}$

Simplify the radical expression.

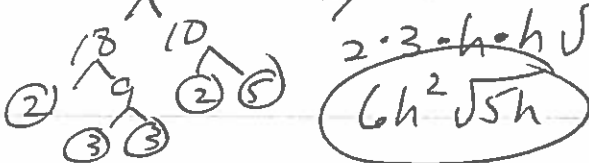
25. $\sqrt{160} = \sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 5}$



OR $\sqrt{16 \cdot 10} = 4\sqrt{10}$

26. $\sqrt{144} = 12$

27. $\sqrt{180h^5} = \sqrt{2 \cdot 2 \cdot 3 \cdot 3 \cdot 5 \cdot (h \cdot h \cdot h \cdot h \cdot h)}$



OR $\sqrt{36 \cdot 5 \cdot h^4 \cdot h} = 6h^2\sqrt{5h}$

Simplify the radical expression.

28. $\sqrt{36g^6} = 6g^3$